# SciPy (linear regression, 1-D and 2-D interpolation) 

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## What we'll cover in this lesson

## 1. SciPy: linear regression

2. SciPy:1-D and 2-D interpolation/regridding

## The SciPy (Scientific Python) package

| scipy.cluster | Vector quantization / Kmeans | Useful constant values (e.g. gravitational constant, Stefan- |
| :---: | :---: | :---: |
| scipy.constants | Physical and mathematical constants | Boltzmann constant) and unit conversions (e.g. nautical miles |
| scipy.fftpack | Fourier transform | to miles) |
| scipy.integrate | Integration routines | Differential equation solvers |
| scipy.interpolate | Interpolation | e'll use this module for 1-D and 2-D interpolation |
| scipy.io | Data input and output | Read and write odd file formats (e.g. MATLAB files) |
| scipy.linalg | Linear algebra routines |  |
| scipy. ndimage | n-dimensional image package |  |
| scipy.odr | Orthogonal distance regression |  |
| scipy.optimize | Optimization |  |
| scipy.signal | Signal processing | Filtering, Fourier/spectral analysis |
| scipy.sparse | Sparse matrices |  |
| scipy.spatial | Spatial data structures and algorithms |  |
| scipy.special | Any special mathematical functions |  |
| scipy.stats | Statistics | I use this module for linear regression |

API reference: https://docs.scipy.org/doc/scipy/reference/index.html
Image credit: scipy-lectures.org

## Loading scipy modules

from scipy import stats
from scipy import interpolate

## Loading scipy modules

from scipy import stats, interpolate

## Does this noisy data have a trend?



## This data has a linear trend and random noise



## Regression relates one (or more) predictor variables

 to a dependent variable, and it requires assuming a "model"Here, a linear model seems appropriate


Here, a linear model is inappropriate (a quadratic model would be better)


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## Regression works by minimizing the square of the errors, so it's sensitive to outliers



The regression line gets "pulled" towards outliers

## Linear regression in SciPy



# If you don't need a function output, you can give it to a "throwaway" underscore 

These output variables will be ignored

slope, intercept, _, _, stderr
$=$ stats.linregress ( $x, y$ )

## Correlation coefficient ( $r$ value) for a linear regression

## Important: the $r$ value is not typically used!

Instead, we use $r^{2}$, which represents the goodness of fit, the proportion of variance $\left(\sigma^{2}\right)$ in the dependent variable $(y)$ that can be predicted from the independent variable $(x)$ by the linear regression model.

- $r^{2}=1.0$ means $100 \%$ of variance is explained by the regression (i.e. the data is a straight line)
- $r^{2}=0.5$ means $50 \%$ of variance is explained by the regression
- $r^{2}=0.0$ means $0 \%$ of variance is explained by the regression (a very poor fit)


## $p$ value for a linear regression

The $p$-value represents the probability of obtaining the given regression slope if the null hypothesis were correct (i.e. the actual slope was zero).

- If $p<0.10$, the null hypothesis of no slope can be rejected at the $90 \%$ confidence level.
- If $p<0.05$, the null hypothesis of no slope can be rejected at the $95 \%$ confidence level.
- If $p<0.01$, the null hypothesis of no slope can be rejected at the $99 \%$ confidence level.

Caution: $p$-values are frequently misused in science.
Small $p$-values can be found even when the chosen model is inappropriate.

## Linear regression results

1 slope, intercept, rvalue, pvalue, stderr = stats.linregress(x,y)
2
3 print('The slope is',round(slope,2))
4 print('The y-intercept is',round(intercept,2))
5 print('The r-value is',round(rvalue,2))
6 print('The p-value is',pvalue)

$$
\begin{aligned}
& y=m x+b+\text { noise } \\
& \text { Slope }(m)=5 \\
& \text { Intercept }(b)=-25
\end{aligned}
$$

7 print('The standard error is',round(stderr,2))
The slope is 5.77
The y-intercept is -28.7
The r-value is 0.53
The $p$-value is $1.779535447617004 \mathrm{e}-08$
The standard error is 0.94


## What if your $x$-values are datetime objects?

```
1 import matplotlib.dates as mdates
2
3 t = np.array([datetime(2020,1,1),\longleftarrow linregress() can'thandle
                                    datetime(2020,2,1), an array of datetime objects
5 datetime(2020,3,1)])
                                    as x-values
t_as_numbers = mdates.date2num(t)
8
9 print(t_as_numbers)
0001-01-01 plus one", which
linregress() can handle
```

[737425. 737456. 737485.]

## What we'll cover in this lesson

1. SciPy: linear regression
2. SciPy: 1-D and 2-D interpolation/regridding

## What is interpolation?

## Definition: Interpolation allows you to estimate unknown values of a variable based on known values of the variable.

## Values of a variable can be unknown because...

- They weren't measured frequently enough in time or space.
- They weren't measured at the right times or locations or on the right grid.
- The data are missing, perhaps because an instrument temporarily stopped measuring.


## Example: climatological high temperatures in Seattle



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## What if we wanted the climatological temperature on November 1?



We'd estimate it using the straight line between the Oct. 15 and Nov. 15 points!

Interpolated ("regridded") from 15th of each month to 1st of each month...


## Interpolation and regridding can come with a loss in accuracy



## 1-D interpolation in SciPy is a two-step process

interp_func $=$ interpolate.interpld(x,y, kind='linear', bounds_error=False, fill_value=np.NaN)
y_new = interp_func(x_new)

## 1-D interpolation in SciPy is a two-step process

This is a function, but you can choose its name
Original $x$ - and $y$-values (1-D arrays)

interp_func $=$ interpolate.interpld( $x, y$,
Other options: 'nearest'
'quadratic', 'cubic ', etc.
If points in $x$ _new are outside $x, \longrightarrow$ bounds er_mor=Ea_se.


Other option: ' extrapolate
y_new = interp_func(x_new)


## Interpolating to/from $x$-values that are datet ime arrays

import matplotlib.dates as mdates interp_func =
 interpolate.interp1d(mdates.date2num(x),y)
y_new $=$ interp_func(mdates.date2num(x_new))

## Types of interpolation



## 2-D interpolation (a.k.a. 2-D regridding)

## You have:

An irregular grid
(l at and lon
ooctatercosdinetes are usually
2-D arrays)



(lat and lon can be represented as 1-D coordinates)

```
plt.pcolormesh()
    plt.contourf()
        xarray's.sel()
```

For more information on regridding, see Climate Data Guide's "Regridding Overview" Image credit: Lu et al. (2018)

## 2-D interpolation in SciPy is a three-step process

```
x_coord = np.linspace(start,end,num_x_points)
y_coord = np.linspace(start,end,num_y_points)
```

x_grid,y_grid = np.meshgrid(x_coord,y_coord)
z_gridded = interpolate.griddata((x_flat,y_flat),
z_flat,
(x_grid,y_grid),
method='linear')

API references: NumPy meshgrid() and SciPy griddata()

## 2-D interpolation in SciPy is a three-step process

Regularly-spaced 1-D coordinate arrays

"Meshed" (stacked) 2-D versions of the 1-D coordinate arrays - compatible with plt.pcolormesh ( ), plt.contourf ( )

Steps \#1 and \#2 are optional if you already have a new $x$ - and $y$-grid

2-D array of the z-parameter values, interpolated to the new $x$ - and $y$-coordinates - compatible with plt.pcolormesh ( ), plt.contourf ()

$$
\text { z_gridded = interpolate.griddata( }\left(x \_f l a t, Y \_f l a t\right),
$$

D arrays of the original irregular $x$ - and $y$-locations and $z$-parameter data


