SciPy (linear regression, 1-D and 2-D interpolation)

Watch by Thursday, November 19, 2020 | Lesson #14

OCEAN 215 | Autumn 2020 Ethan Campbell and Katy Christensen

What we'll cover in this lesson

SciPy: linear regression SciPy: 1-D and 2-D interpolation/regridding

The SciPy (Scientific Python) package

<pre>scipy.cluster</pre>	Vector quantization / Kmeans	Useful constant values (e.g. gravitational constant, Stefa
<pre>scipy.constants</pre>	Physical and mathematical constants	Boltzmann constant) and unit conversions (e.g. nautical
<pre>scipy.fftpack</pre>	Fourier transform	to miles)
<pre>scipy.integrate</pre>	Integration routines	Differential equation solvers
<pre>scipy.interpolate</pre>	Interpolation	— We'll use this module for 1-D and 2-D interpolation
scipy.io	Data input and output	Read and write odd file formats (e.g. MATLAB files)
<pre>scipy.linalg</pre>	Linear algebra routines	
<pre>scipy.ndimage</pre>	n-dimensional image package	
scipy.odr	Orthogonal distance regression	
<pre>scipy.optimize</pre>	Optimization	
<pre>scipy.signal</pre>	Signal processing	Filtering, Fourier/spectral analysis
<pre>scipy.sparse</pre>	Sparse matrices	
<pre>scipy.spatial</pre>	Spatial data structures and algorithms	
<pre>scipy.special</pre>	Any special mathematical functions	
<pre>scipy.stats</pre>	Statistics	— We'll use this module for linear regression
		Also available: statistical tests (t-test, chi-squared test)
API reference: https://do	<u>ocs.scipy.org/doc/scipy/reference/index.h</u>	<u>Image credit: scipy-lecture</u>





Loading scipy modules

from scipy import stats from scipy import interpolate

Loading scipy modules

from scipy import stats, interpolate



Does this noisy data have a trend?



This data has a linear trend and random noise



Х

Regression relates one (or more) predictor variables to a dependent variable, and it requires assuming a "model"

Here, a linear model seems appropriate



Here, a linear model is inappropriate (a **quadratic model** would be better)





Regression relates one (or more) predictor variables to a dependent variable, and it requires assuming a "model"

Here, a linear model seems appropriate







Regression works by minimizing the square of the errors, so it's sensitive to outliers





Linear regression in SciPy

= stats.linregress(x,y)

1-D NumPy arrays of the same length



If you don't need a function output, you can give it to a "throwaway" underscore

= stats.linregress(x,y)



Correlation coefficient (*r* value) for a linear regression

- Instead, we use r^2 , which represents the **goodness of fit**, the proportion of variance (σ^2) in the dependent variable (y) that can be predicted from the independent variable (x) by the linear regression model.
- $r^2 = 1.0$ means 100% of variance is explained by the regression (i.e. the data is a straight line)
- $r^2 = 0.5$ means 50% of variance is explained by the regression
- $r^2 = 0.0$ means 0% of variance is explained by the regression (a very poor fit)

Important: the *r* value is not typically used!

p value for a linear regression

- The *p*-value represents the probability of obtaining the given regression slope if the null hypothesis were correct (i.e. the actual slope was zero).
- If p < 0.10, the null hypothesis of no slope can be rejected at the 90% confidence level.
- If p < 0.05, the null hypothesis of no slope can be rejected at the 95% confidence level.
- If p < 0.01, the null hypothesis of no slope can be rejected at the 99% confidence level.
 - **Caution:** *p*-values are frequently misused in science. Small *p*-values can be found even when the chosen model is inappropriate.

Linear regression results

```
1 slope, intercept, rvalue, pvalue, stderr = stats.linregress(x,y)
2
3 print('The slope is',round(slope,2))
4 print('The y-intercept is',round(intercept,2))
5 print('The r-value is',round(rvalue,2))
6 print('The p-value is',pvalue)
7 print('The standard error is',round(stderr,2))
80
```

```
The slope is 5.77
The y-intercept is -28.7
The r-value is 0.53
The p-value is 1.779535447617004e-08
The standard error is 0.94
```


What if your x-values are datetime objects?

1 import matplotlib.dates as mdates 2 3 t = np.array([datetime(2020,1,1), + linregress() can't handle datetime(2020,2,1), an array of datetime objects 4 as x-values datetime(2020,3,1)]) 5 6 $7 t_as_numbers = mdates_date2num(t)$ This converts datetime objects to numbers representing "days since 8 0001-01-01 plus one", which 9 print(t_as_numbers) linregress() can handle

[737425. 737456. 737485.]

What we'll cover in this lesson

1. SciPy: linear regression 2. SciPy: 1-D and 2-D interpolation/regridding

What is interpolation?

Definition: Interpolation allows you to estimate unknown values of a variable based on known values of the variable.

Values of a variable can be unknown because...

- They weren't measured frequently enough in time or space.
- They weren't measured at the right times or locations or on the right grid.
- The data are missing, perhaps because an instrument temporarily stopped measuring.

Example: climatological high temperatures in Seattle

Example: climatological high temperatures in Seattle

What if we wanted the climatological temperature on November 1?

Interpolated ("regridded") from 15th of each month to 1st of each month...

Climatological high temperatures in Seattle Original Interpolated Sep Nov Jul Jan Month

ו...

Interpolation and regridding can come with a loss in accuracy

1-D interpolation in SciPy is a two-step process

interp func = interpolate.interpld(x,y, kind='linear', bounds error=False, fill value=np.NaN)

y new = interp func(x new)

API reference: <u>SciPv interp1d()</u>

1-D interpolation in SciPy is a two-step process

This is a function, but you can choose its name

Other options: 'nearest', 'quadratic', 'cubic', etc.

> If points in x new are outside x, set to False to avoid an error

Other option: 'extrapolate

interp func(x new)

Interpolated y-values (1-D array)

Set of x-values to interpolate to (1-D array)

Original x- and y-values (1-D arrays) interp func = interpolate.interpld(x,y, * kind='linear', bounds error=False,

fill value=np.NaN)

Interpolating to/from x-values that are datetime arrays

import matplotlib.dates as mdates

interp func =

y_new = interp func(mdates.date2num(x new))

Converts datetime objects into numbers of days

interpolate.interpld(mdates.date2num(x),y)

Types of interpolation

2-D interpolation (a.k.a. 2-D regridding)

For more information on regridding, see <u>Climate Data Guide's "Regridding Overview"</u> Image credit: <u>Lu et al. (2018)</u>

2-D interpolation in SciPy is a three-step process

x coord = np.linspace(start,end,num x points) y coord = np.linspace(start,end,num y points)

x grid,y grid = np.meshgrid(x_coord,y_coord)

API references: <u>NumPy meshgrid()</u> and <u>SciPy griddata()</u>

z gridded = interpolate.griddata((x flat, y flat), z_flat, (x_grid,y_grid), method='linear')

2-D interpolation in SciPy is a three-step process

