# Watch by Tuesday, October 20, 2020 । Lesson \#5 

## NumPy

## Arrays and functions

OCEAN 215 | Autumn 2020
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## What we'll cover in this lesson

## 1. Functions and arguments

2. NumPy arrays - arithmetic, logical operations, indexing
3. NumPy functions and constants

## Functions and arguments

Function name An "argument" or "parameter"


The function "returns" or "evaluates to" the integer 4

## Some functions act on a target

The "target" of the function


The function returns ' PYTHON '

## Values returned by functions can be stored in a variable


new_string $=$ 'python'.upper()

# Some functions don't return anything 

## numbers $=[6,8,7,5]$

## numbers.sort ()

This function returns nothing at all!
It simply modifies numbers "in-place," which becomes $[5,6,7,8$ ].

## Some functions have named arguments

## "Named" or "keyword" argument Argument value <br>  <br> numbers.sort(reverse=True)

Now, numbers will be sorted in reverse order: [ $8,7,6,5$ ].

# Named arguments always have a default value 

The "default" value of reverse

## numbers.sort(reverse=False)

is equivalent to:

## numbers.sort()

## Functions can have both positional and named arguments

## "Positional" arguments have a fixed order


function_name(arg1, arg2, arg3,..., named_arg1=default1, named_arg2=default2,...)

"Named" arguments can be provided in any order, but they must follow any positional arguments

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## Loading NumPy ("Numeric Python")

Makes this package available to Python


Package names are usually all lowercase

## import numpy

This is a shortcut; you can choose any name but np is most common 1 as np

This part is technically optional

## Checking a package's version

## 1 import numpy as np <br> 2 <br> 3 print(np.__version__) <br> $$
\Gamma \quad 1.18 .5
$$ <br> That's a double underscore:

## The NumPy array (ndarray)

" N -dimensional array" (e.g. 1-D, 2-D, 3-D, 4-D, etc.)

## np.array([5, 6, 7, 8])

## Similarities between lists and NumPy 1-D arrays

Both are mutable (they can be changed)

```
1 numbers = np.array([5,6,7,8])
2 numbers[1] = 13
3 print(numbers)
```

```
C] [ 5 13 % 7 8]
```

Both are iterable
1 for num in numbers:
2 print (num)
[ 5
13
7
8

Both are compatible with indexing and slicing
1 print(numbers[-3:])
$\left[\rightarrow \quad\left[\begin{array}{lll}13 & 7 & 8\end{array}\right]\right.$

Find length using len ()
1 print(len(numbers))
[ 7

Check membership using in and not in
1 print(13 in numbers)
2 print(14 in numbers)
$\square \rightarrow$ True
False

## Differences between lists and NumPy 1-D arrays

## Lists

- Lists can contain a mix of object types (integers, strings, sub-lists, etc.)


## NumPy 1-D arrays

- Arrays can contain only a single object type (check using . dtype, change using .astype())

1 numbers = np.array( $[5,6,7,8])$
2 print(numbers.dtype)
3 print(numbers.astype(str))
[ $]$ int64
['5' '6' '7' '8']

- Arrays are fast for computation and small in memory (great for big data)


## Differences between lists and NumPy 1-D arrays

Lists

- Lists don't preserve scientific notation in floating-point numbers

1 print([3.5e9,1.4e-3])
[ $] \quad[3500000000.0,0.0014]$

- Use Python's in-place append ( ) or extend(),insert(), del, reverse(), remove(), pop()

1 numbers = [5,6,7,8]
2 numbers.append( $[9,10]$ )
3 print(numbers)
$[\overrightarrow{[ } \quad[5,6,7,8,[9,10]]$

## NumPy 1-D arrays

- Arrays preserve scientific notation

```
1 print(np.array([3.5e9,1.4e-3]))
[-> [3.5e+09 1.4e-03]
```

- NumPy's append(), insert(), delete(), flip() functions are not in-place; note the different syntax; no functions to remove, pop
1 numbers = np.array([5,6,7,8])
2 numbers = np.append(numbers, [9,10])
3 print(numbers)
$\stackrel{[ }{\square} \quad\left[\begin{array}{llllll}5 & 6 & 7 & 8 & 9 & 10\end{array}\right]$


## Differences between lists and NumPy 1-D arrays

Lists

- Convert from list $\rightarrow$ array using:

1 my_list = [5, 6, 7, 8]
2 my_array = np.array(my_list)

- Adding lists concatenates (joins) them:

1 a = [1,2,3,4]
2 b = [5,6,7,8]
3 print (a + b)
$[\rightarrow \quad[1,2,3,4,5,6,7,8]$

## NumPy 1-D arrays

- Convert from array $\rightarrow$ list using:

1 my_list1 = my_array.tolist()
2 my_list2 = list(my_array)

- Adding arrays actually adds them!*

1 a = np.array([1,2,3,4])
2 b = np.array([5,6,7,8])
3 print (a + b)
[ $\rightarrow$ [ 6 8 10 12]

* Note that NumPy also has a concatenate ( ) function.


## Arithmetic operations with arrays

Arithmetic operators

| + | Addition |
| :---: | :---: |
| _ | Subtraction |
| * | Multiplication |
| / | Division |
| ** | Exponential |
| \% | Remainder |
| / / | Floor |

Element-wise arithmetic between two or more arrays
1 a = np.array $([1,2,3,4])$
2 b = np.array([5,6,7,8])
3
4 print('a + b =', a + b)
$a+b=\left[\begin{array}{llll}6 & 8 & 10 & 12\end{array}\right]$
5 print('a - b =',a - b)
$\mathrm{a}-\mathrm{b}=\left[\begin{array}{llll}-4 & -4 & -4 & -4\end{array}\right]$
6 print('a * b =', a * b)
$\mathrm{a} * \mathrm{~b}=\left[\begin{array}{llll}5 & 12 & 21 & 32\end{array}\right]$

Element-wise arithmetic with an array and a number

```
1 print('a + 10 =',a + 10)
2 print('10 * a =',10 * a) 10 * a = [10 20 30 40]
a + 10 = [lllllll}11213 14]
3 print('a / 10 =',a / 10) a / 10 = [0.1 0.2 0.3 0.4]
4 print('a**2 =',a**2)
```


## Element-wise operations require arrays to be the same dimensions

```
1 x = np.array([1,2,3])
2 y = np.array([11,12,13,14,15])
3
4 \text { print(x+y)}
```

[

```
ValueError
<ipython-input-97-d5d99ad6233b> in <module>()
    2 y = np.array([11,12,13,14,15])
    3
----> 4 print(x + y)
```

Traceback (most recent call last)

ValueError: operands could not be broadcast together with shapes (3,) (5,)

## Logical operations with arrays

Comparison operators

| $==$ | Equal |
| :---: | :---: |
| $\mathbf{=}$ | Not equal |
| $>$ | Greater than |
| $>=$ | Greater than or <br> equal to |
| $<$ | Less than |
| $<=$ | Less than or <br> equal to |

Element-wise comparisons between two arrays or an array and a number

```
1 u = np.array([1,2,3,4])
2 v = np.array([0,2,4,6])
3
```

4 print(u == v) [False True False False]
5 print(u < v) [False False True True]
6 print(v != 0) [False True True True]
7 print $(v<=4) \quad[$ True True True False]

Instead of comparing Boolean arrays with and/or, use np.logical_and () and np.logical_or()

1 bool1 = np.array([True,False,True])
2 bool2 = np.array([True,False,False])
3
4 print(np.logical_and(bool1,bool2)) [ True False False]
5 print(np.logical_or(bool1,bool2)) [ True False True]

## New indexing options with arrays

When you want to access certain value(s) in an array:

```
1 v = np.array([10,11,12,13]) Python prints:
2
3 print(v[3]) 13
4
print(v[[2,3]])
6
7 print(v[v >= 12])
8
9 print(v[[False,False,True,True]]) [12 13] ... because they evaluate to Boolean arrays
```

[12 13] Multiple indices retrieves multiple elements
[12 13] Logical conditions also work...
[ 12 13] ... because they evaluate to Boolean arrays
When you want the indices of certain values in an array:

```
```

print(np.where(v >= 12)) (array([2, 3]),)

```
```

print(np.where(v >= 12)) (array([2, 3]),)
3 print(np.where(v >= 12)[0]) [2 3]

```
```

3 print(np.where(v >= 12)[0]) [2 3]

```
```

    np. where ( ) gives the indices at which a Boolean condition is satisfied...
    When you want the indices of certain values in an array:
... but you have to index into the result using [ 0 ]

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## Most functions acting on NumPy arrays can be called two ways

```
x = np.array([10,11,12,13])
```

np.sum (X) $\longleftarrow$ Evaluates to: 46
x.sum ()
« Evaluates to: 46

# NumPy functions can also be applied to lists 

$$
x=[10,11,12,13]
$$

np.sum (x)
〔 Evaluates to: 46
X.sum ()
$\longleftarrow$ Evaluates to: 46

## Mathematical reductions (array $\rightarrow$ number)

$$
x=n p \cdot \operatorname{array}([10,11,12,13])
$$

## Function:

```
np.sum(x)
np.mean(x)
np.median(x)
np.max(x)
np.min(x)
np.std(x)
```

Purpose:
Sum
Mean (average)
Median
Maximum value
Minimum value
Standard deviation

## Evaluates to:

46
11.5
11.5

13
10
1.11803...

## Mathematical constants (each return a float)

## Constant value:

np.pi
np.e
np.inf
np.nan

## Purpose:

$\pi$ (pi)
$e$ (Euler's number)
Positive infinity
"Not a Number"
(used as a placeholder for missing data)

## Evaluates to:

3.14159...
2.71828...
inf
nan

Note:

$$
\begin{aligned}
& 1 \text { print(5 * np.inf) } \\
& 2 \text { print(5 * np.nan) }
\end{aligned} \quad \sqsubset \quad \begin{array}{ll}
\inf \\
\text { nan }
\end{array}
$$

## Element-wise functions (number $\rightarrow$ number, or array $\rightarrow$ array)

## Function:

```
np.absolute([-2,-1])
np.round([5.23,5.29],1)
np.sqrt([4,9,16])
np.exp([0,1,2])
np.sin([0,np.pi/2])
```

np.cos([np.pi,2*np.pi]) Cosine

## Purpose:

Absolute value
Round to a certain decimal place
Square root
(same as **0.5)
Exponential
(same as np.e**)
Sine (from radians) [0.,1.]

Cosine

## Evaluates to arrays:

[2,1]
[5.2,5.3]
[2.,3.,4.]
[1., 2.718..., 7.389...]
[-1.,1.]

## Functions to create new arrays

## Function:

np.zeros(4)
np.ones(4)
np.full(4,2)
np.arange(4)
np.arange ( $0,1,0.25$ )
np.linspace (0,1,5)

## Purpose:

Array of given length filled with zeros
Array of given length filled with ones
Array of given length filled with given value

Same as range ( )...
...except floats and fractional increments are allowed

Returns the given number of evenly spaced values from start to end (both are inclusive)

## Evaluates to arrays:

[0.,0.,0.,0.]
[1.,1.,1.,1.]
$[2,2,2,2]$
$[0,1,2,3]$
$[0 ., 0.25,0.5,0.75]$
$[0 ., 0.25,0.5,0.75,1$.

